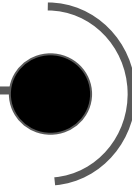
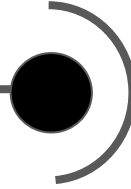


# Reconciling approaches to address model performance and interdependency in CMIP6



**Ben Sanderson, NCAR**

Earth System Model Evaluation to Improve  
Process Understanding, Aspen, 2017



## Bayesian Worldview

IPCC AR5  
Tebaldi et al (2005,2009)

## Replicate Earth Paradigm

Bishop & Abramowitz  
(2013)

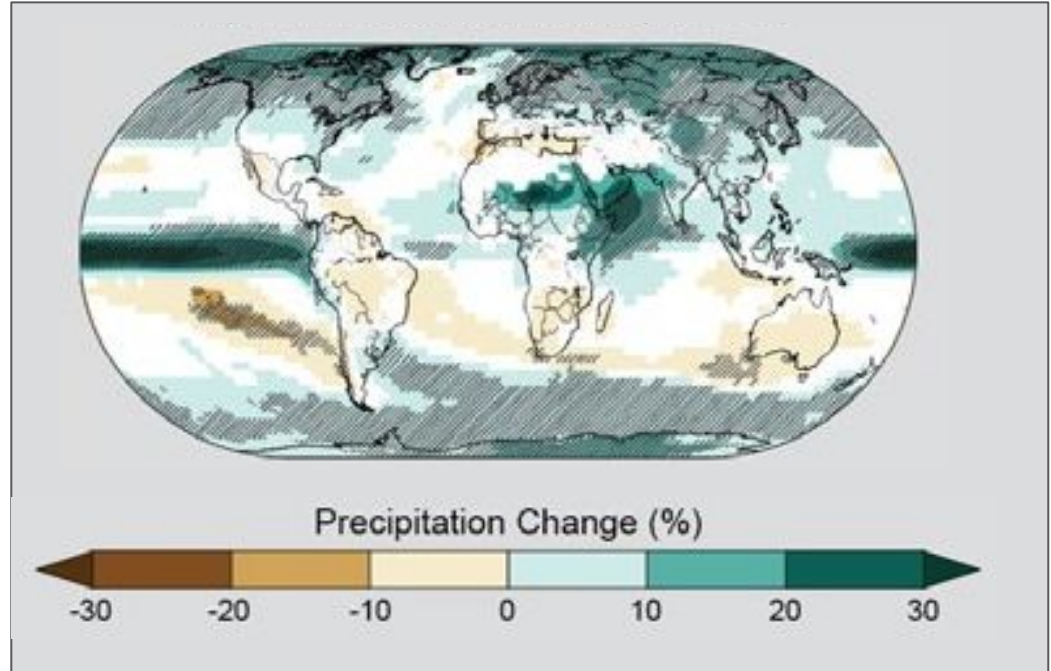
## Geometric Worldview

Sanderson (2015a,b, 2017)  
Knutti (2017)

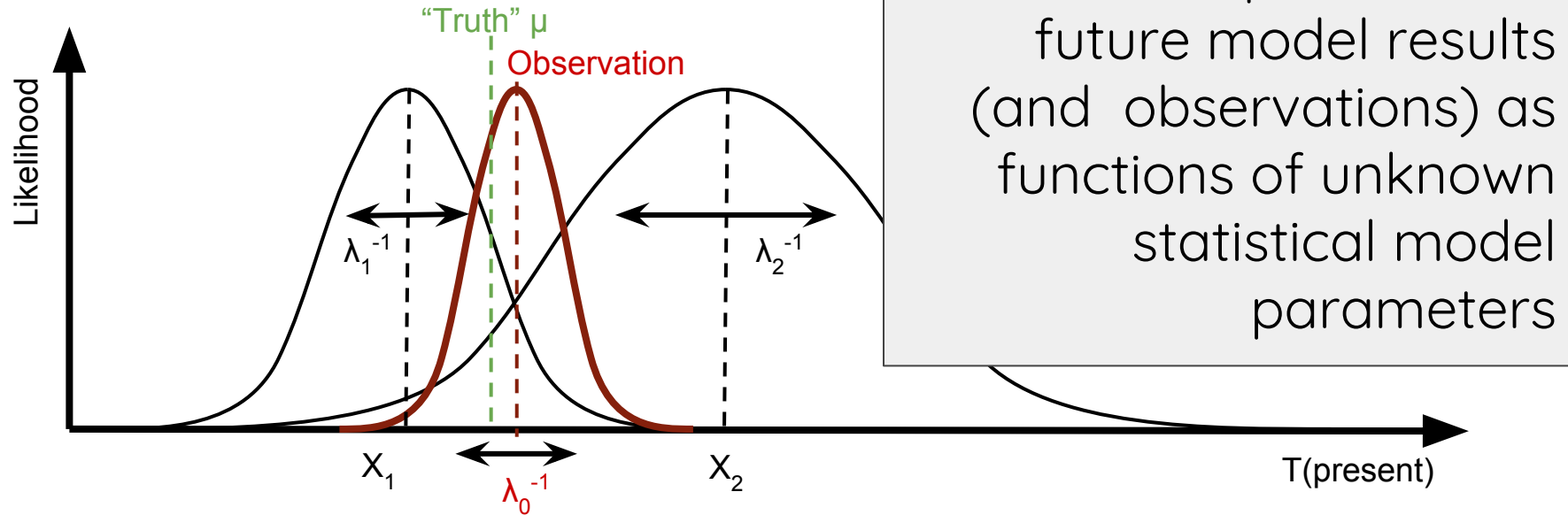
## Bayesian Worldview

Ensemble members are observations or samples of the true state of the climate system. Additional models in agreement will improve confidence in the most likely future climate.

IPCC AR5  
Tebaldi et al (2005,2009)



# Accounting for model skill: the Bayesian approach



In the fashion of Tebaldi et al (2005)

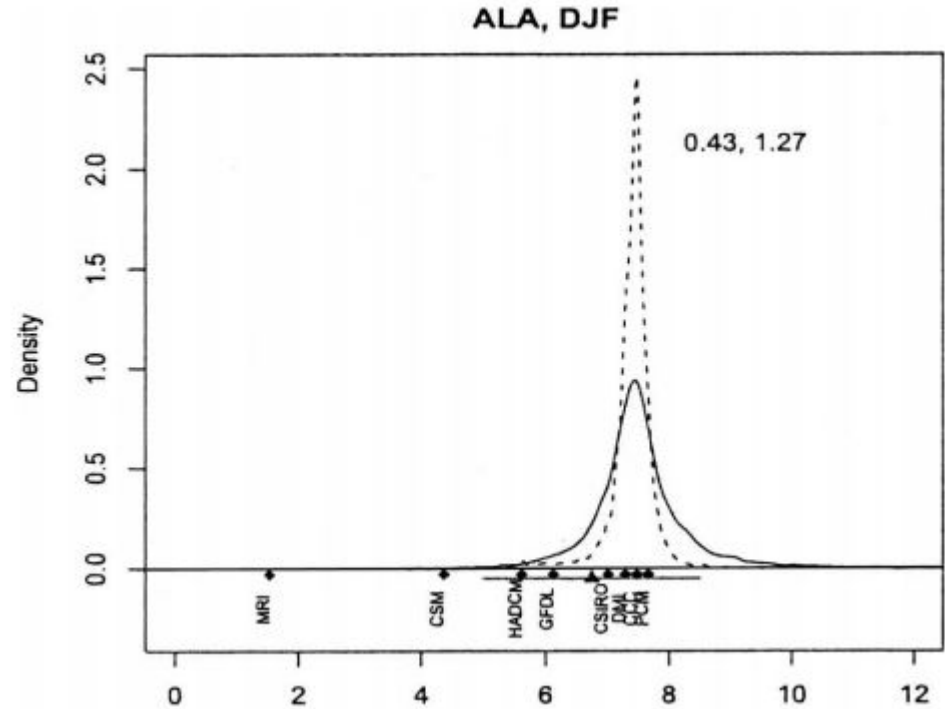
## Assumptions

# Bayesian Worldview

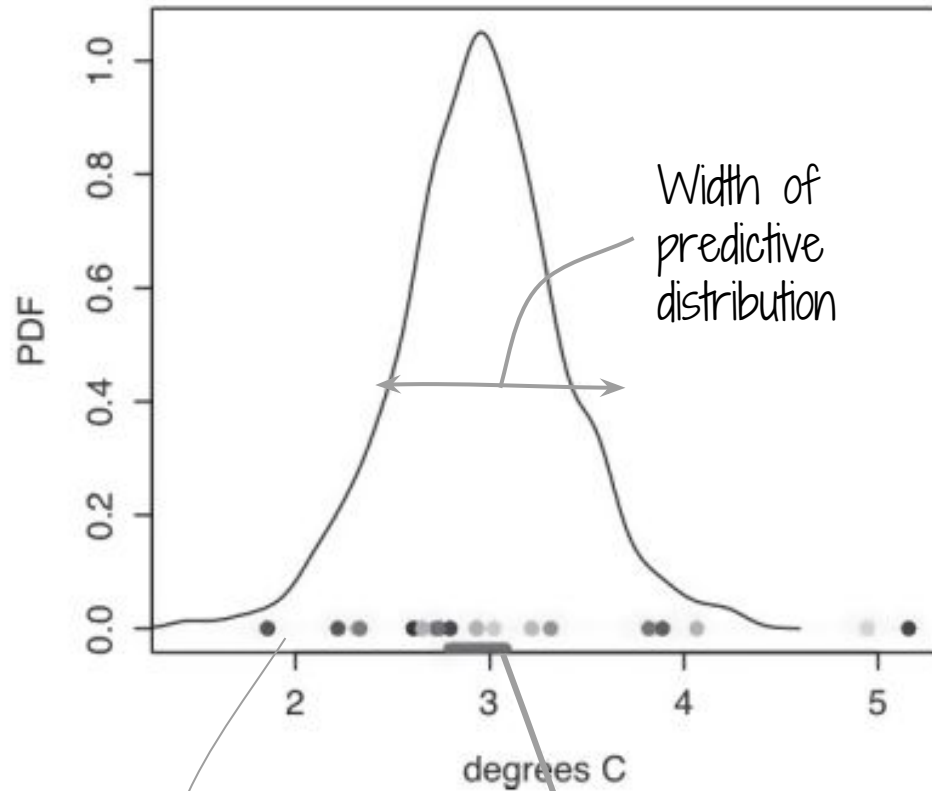
IPCC AR5  
Tebaldi et al (2005,2009)

- 1) More models in agreement imply more confidence in projection
- 2) Each model is an equally plausible representation the true system
- 3) Present-day performance can be informative about future behavior

Monte-Carlo  
Sampling over  
self-consistent  
parameter sets in  
posterior distribution  
yields PDFs for  
model parameters.  
Large number of  
models -> very low  
spread in projection



Tebaldi et al (2005)

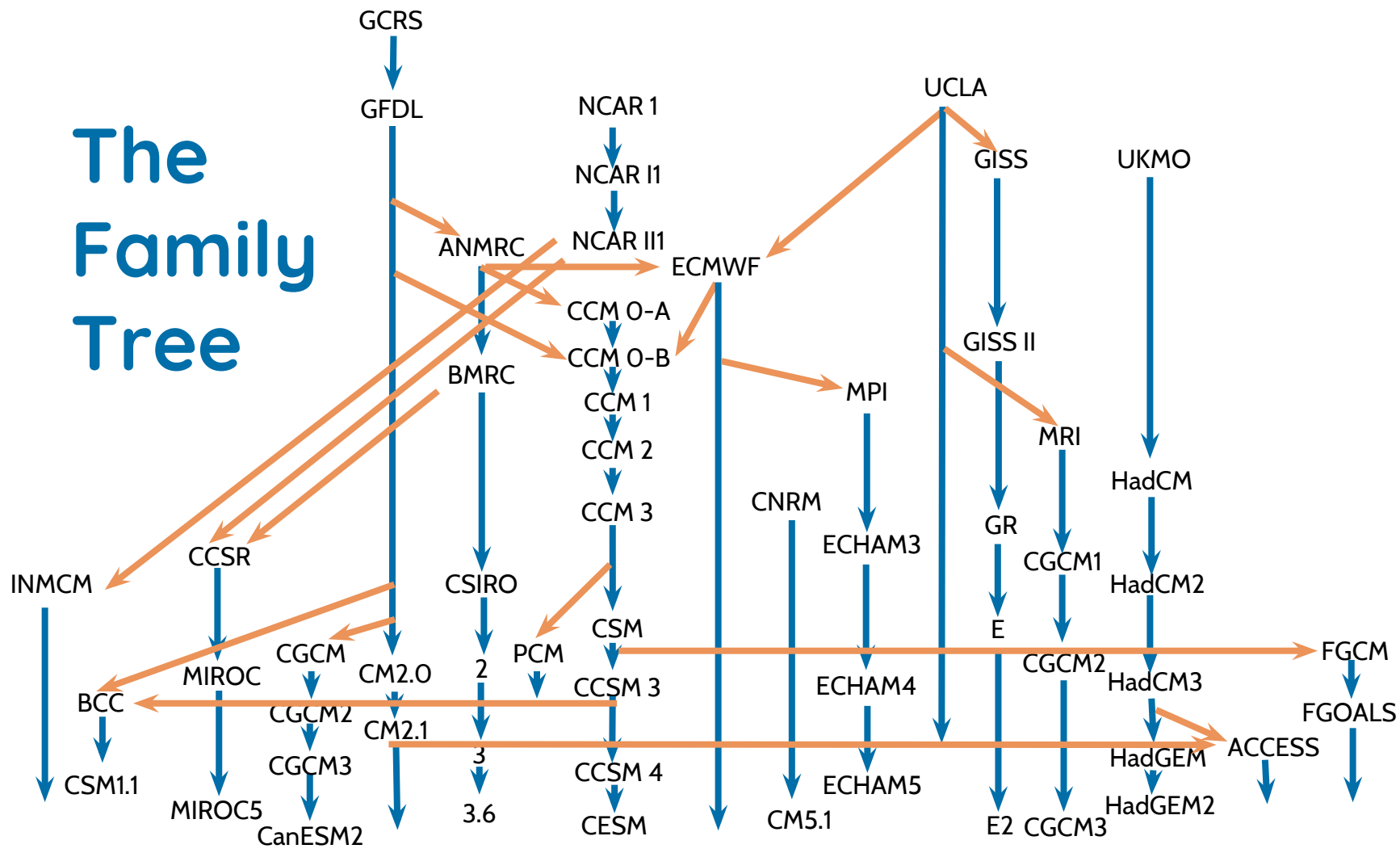


Original model  
projections of  
warming

Uncertainty in  
mean projection

A predictive  
distribution  
considers possible  
plausible states of  
the real system,  
informed by the  
prior of CMIP  
model precision

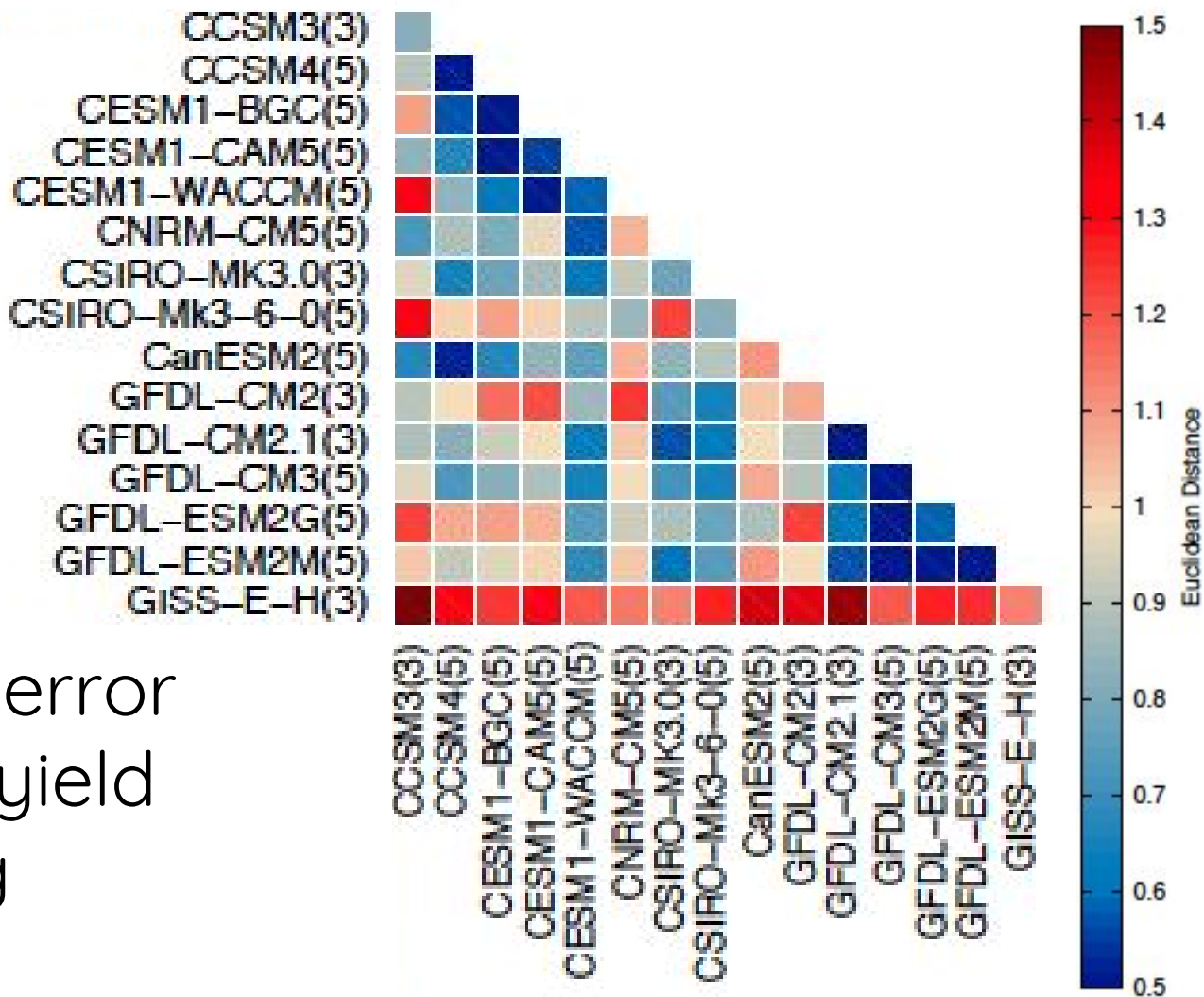
Tebaldi *et al* (2009)

[illegible]

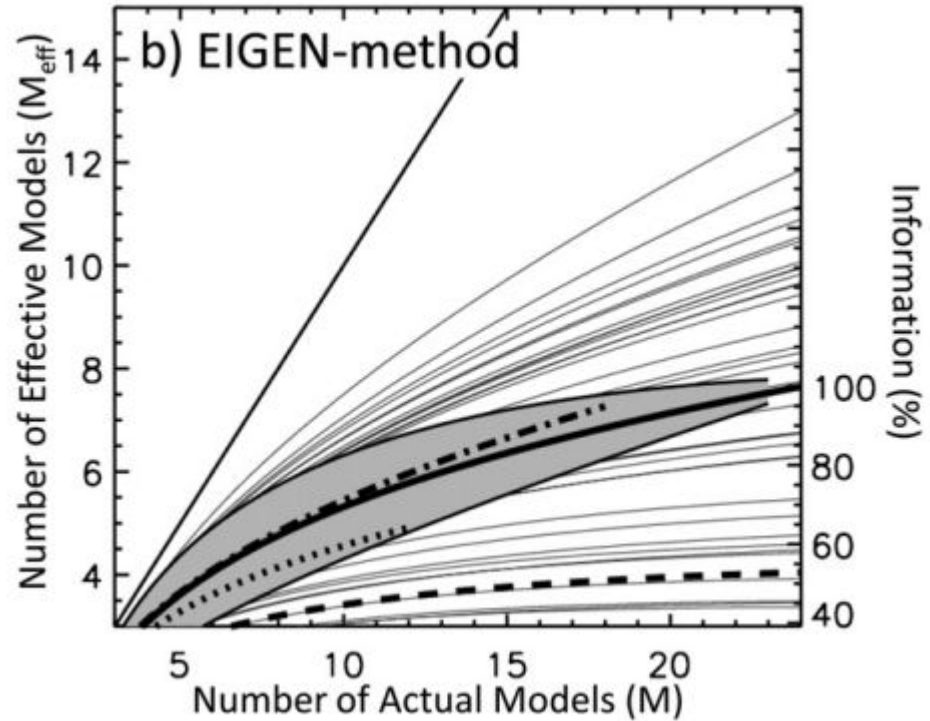


From Sanderson  
*et al* (2015a)

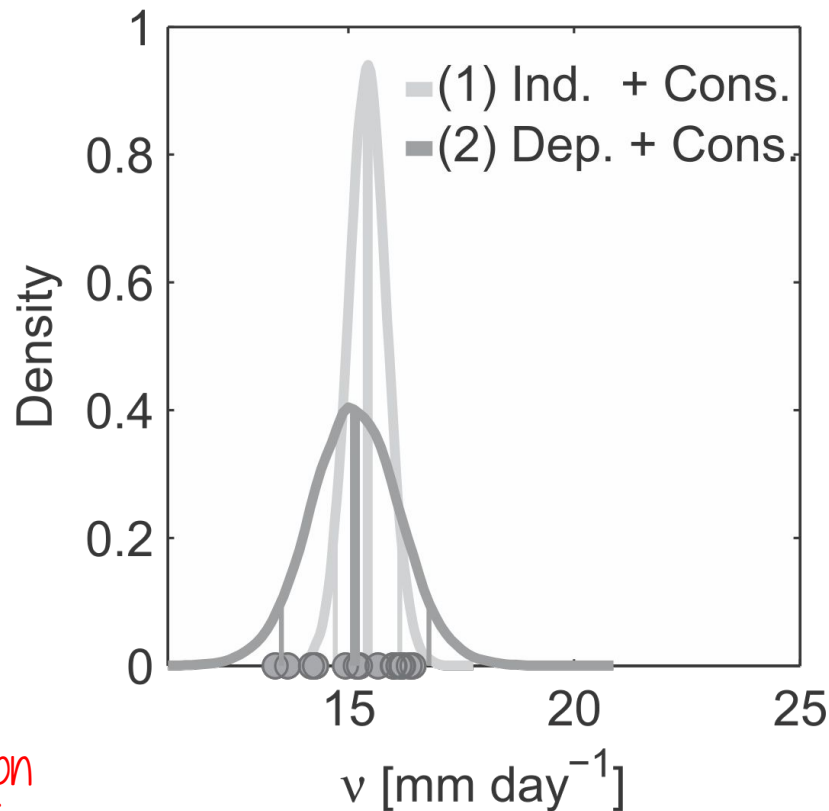
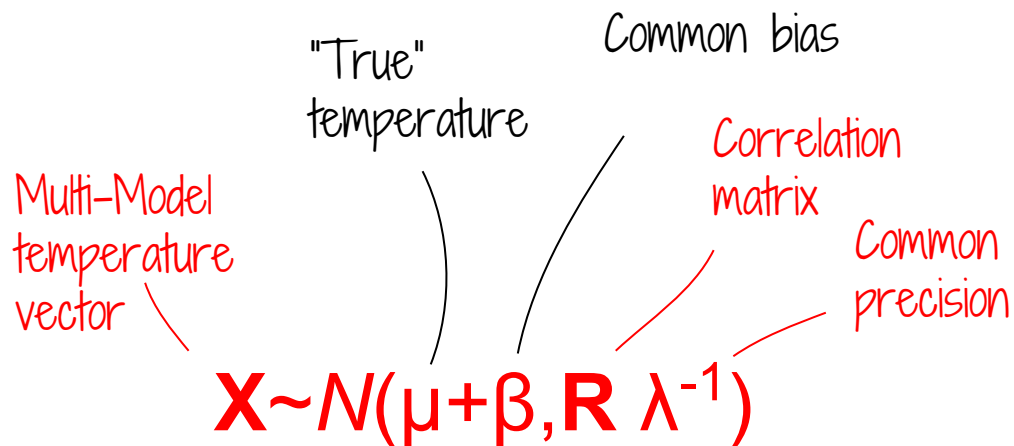
Inter-model  
distances (or error  
correlations) yield  
an underlying  
structure...



Eigen-analysis of this matrix suggests that the number of effective models may be smaller than the number of actual models...



Solution 1: assume models are **correlated**, drawn from a multivariate distribution



Sunyer *et al* (2014)

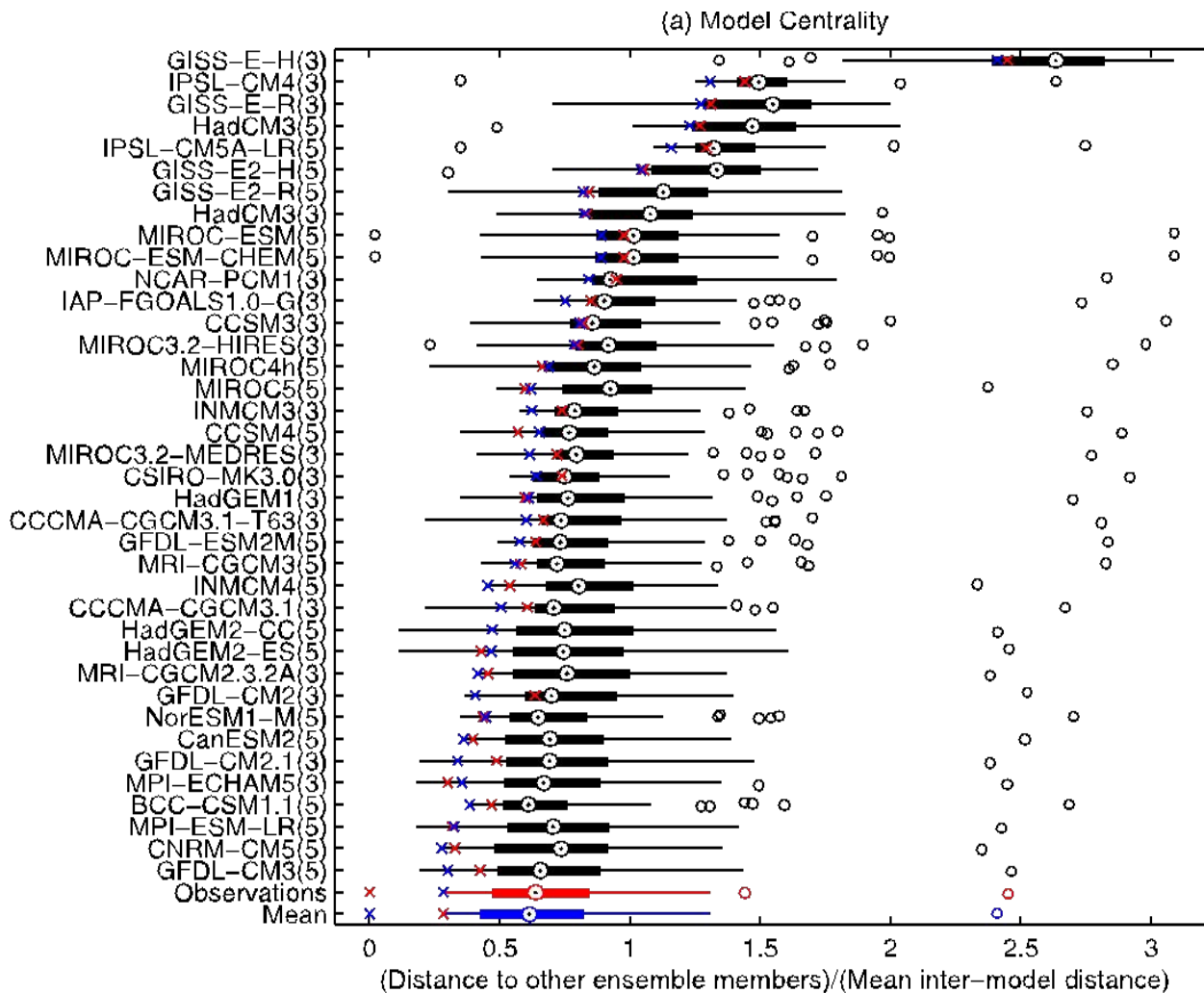
# Bayesian Worldview

IPCC AR5  
Tebaldi et al (2005,2009)

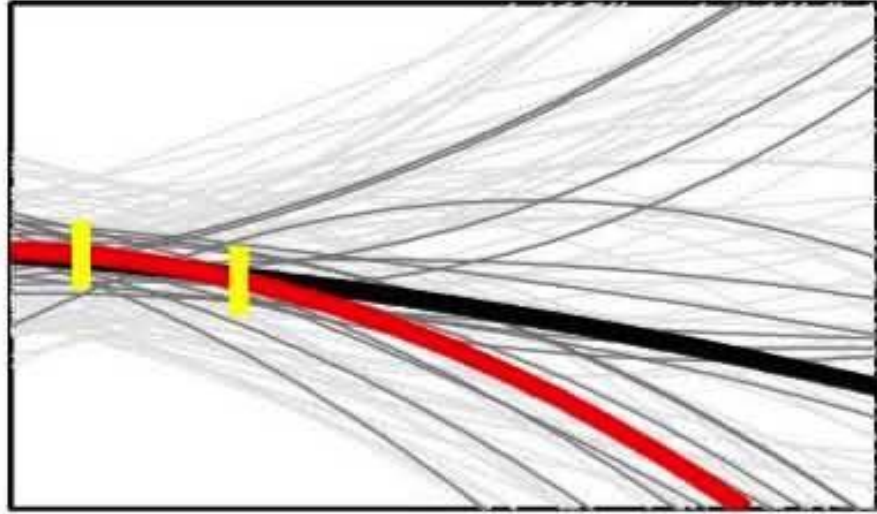
- 1) More **independent** models in agreement implies more confidence in **mean** projection
- 2) Each model is an equally plausible representation of the true system
- 3) Present-day performance can be informative about future behavior

Models are  
in general  
closer to obs  
than **any**  
other  
model...

Sanderson and  
Knutti (2012)



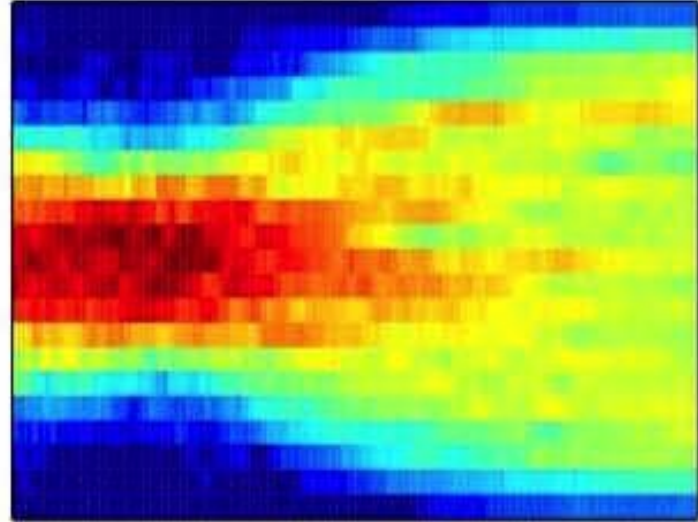
Present day apparent truth-centeredness can be an artifact of **tuning**



Time

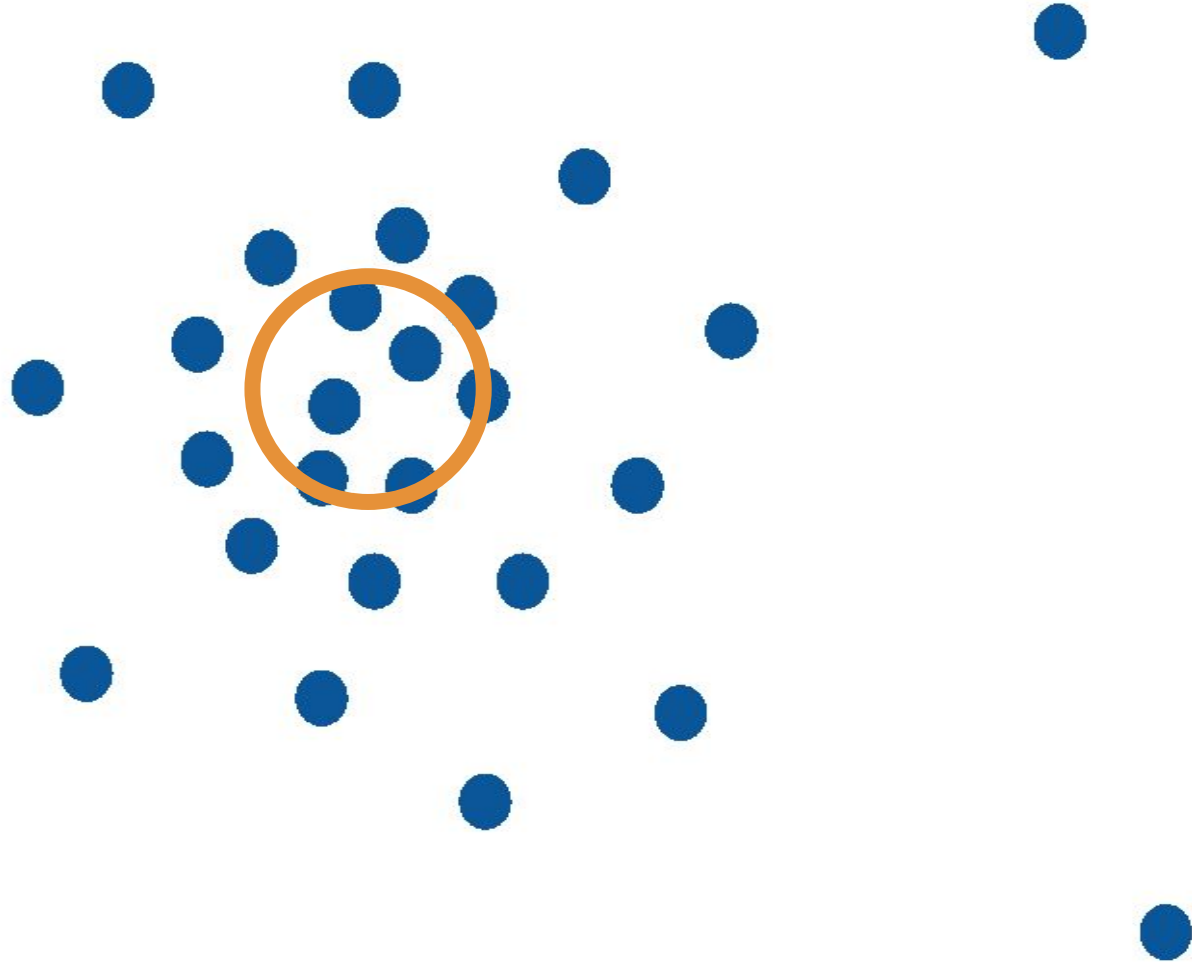
Sanderson and Knutti (2012)

Rank

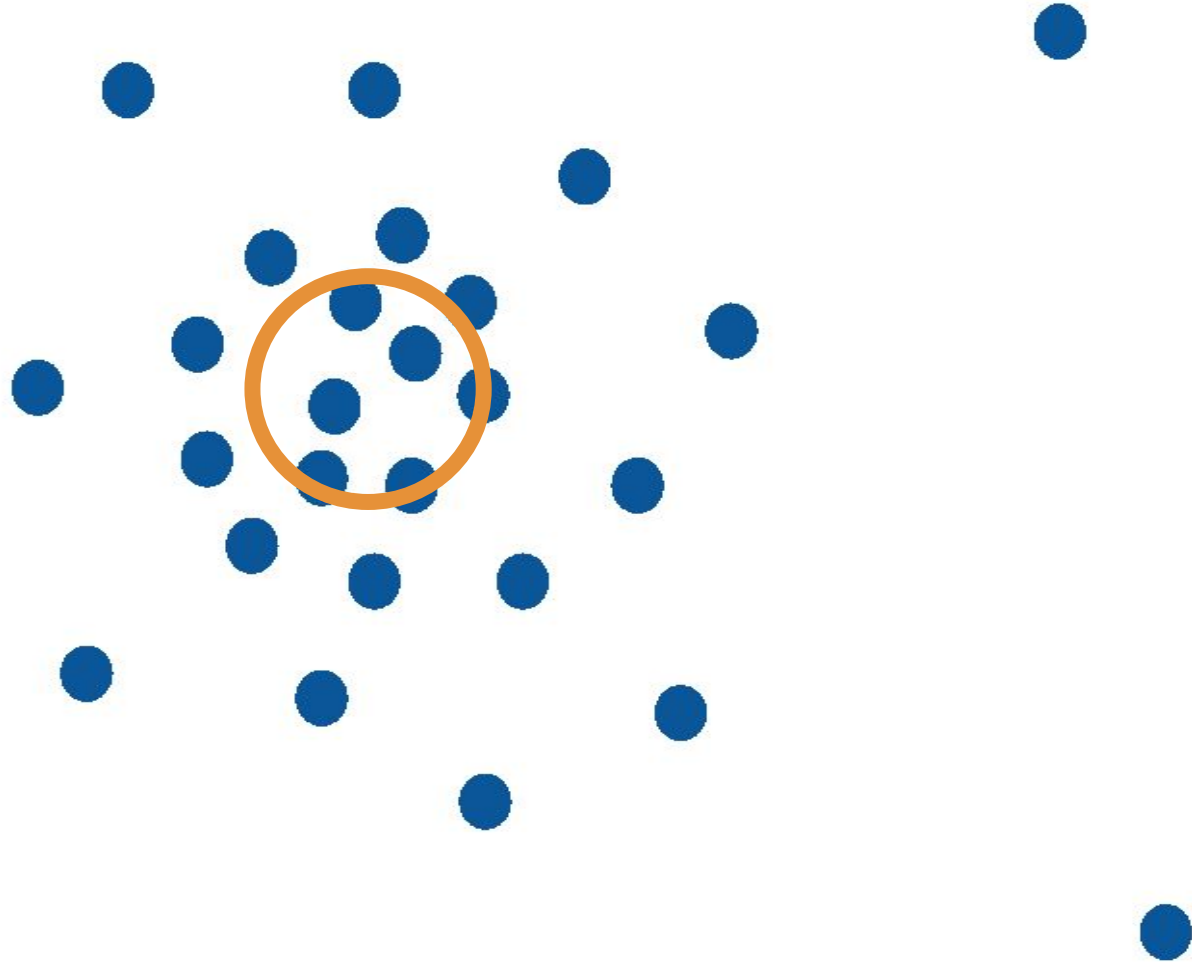


Time

So CMIP5 **is**  
weakly truth  
centered  
(historically,  
perhaps due to  
tuning), with  
some poorly  
performing  
outliers...



... so should  
a sufficiently  
**poor** outlier  
influence  
any  
combined/w  
eighted  
projection?





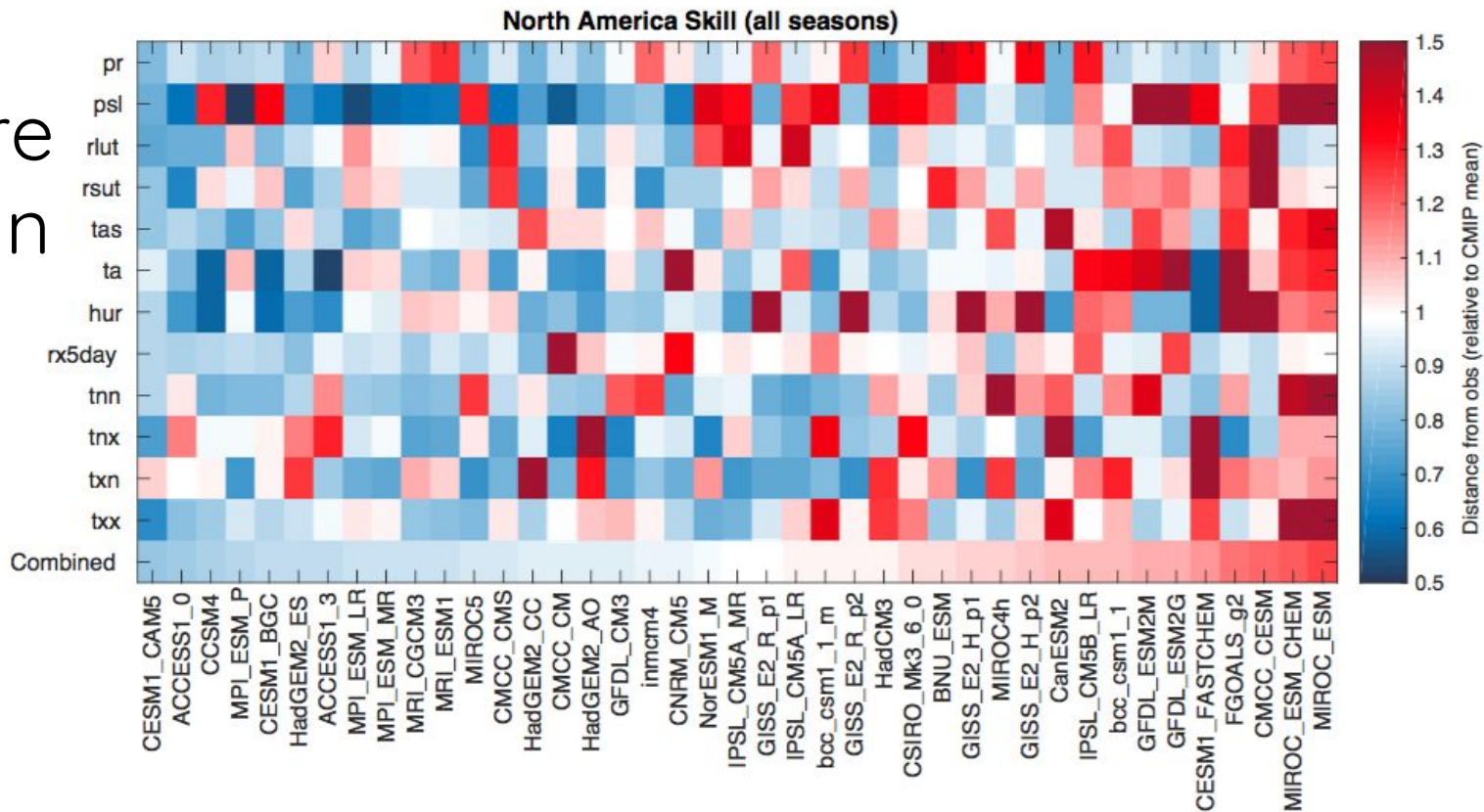
## Assumptions

# Bayesian Worldview

IPCC AR5  
Tebaldi et al (2005,2009)

- 1) More **independent** models in agreement implies more confidence in mean projection (**fixable**)
- 2) Each model is an equally plausible representation of the true system (**not generally true, tuning overstates agreement, very poor models would overinflate uncertainty**)
- 3) Present-day performance can be informative about future behavior

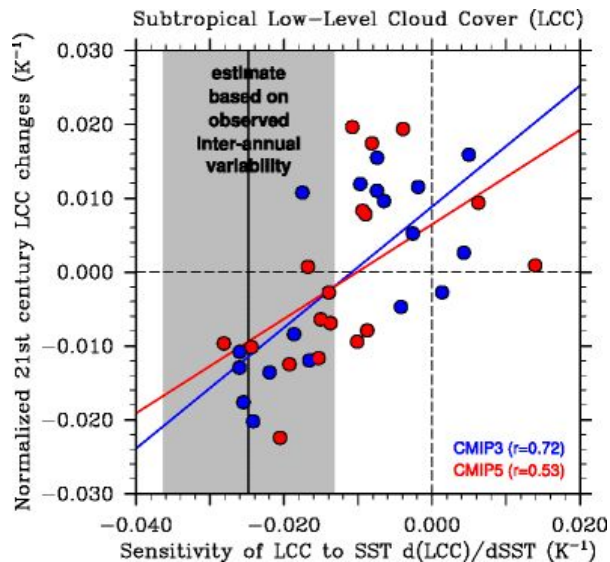
Some models are better than others (but the winner depends on what you look at...)



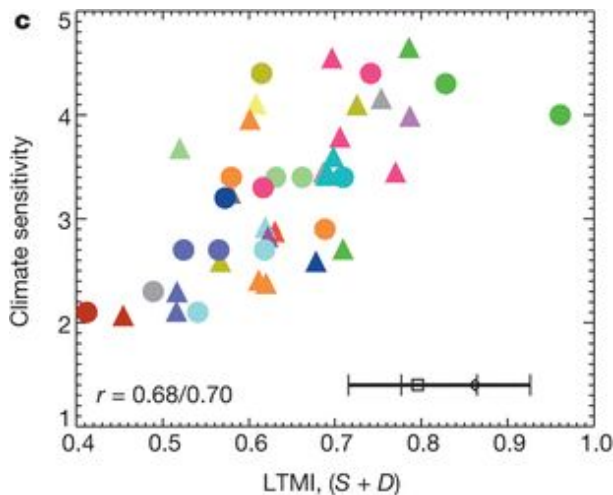
Sanderson *et al* (2017)

Emergent constraints have yet to be posed in a comprehensive, multivariate probabilistic framework.

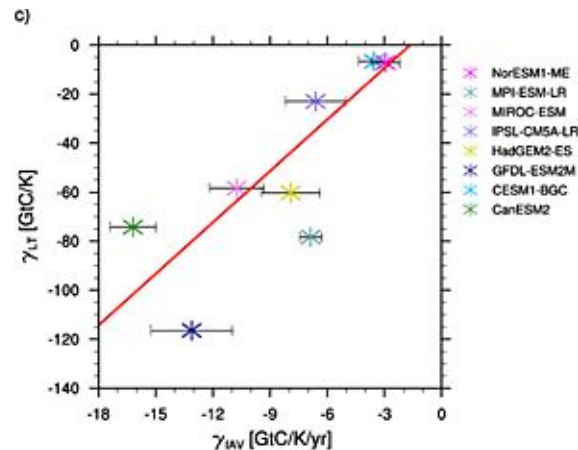
Qu et al (2014)



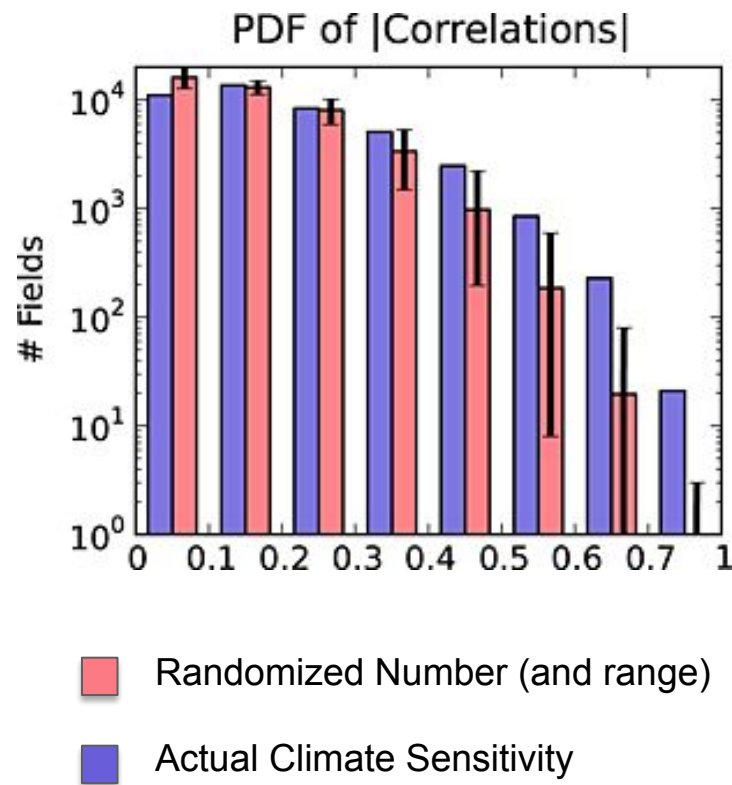
Sherwood et al (2014)



Wenzel et al (2014)

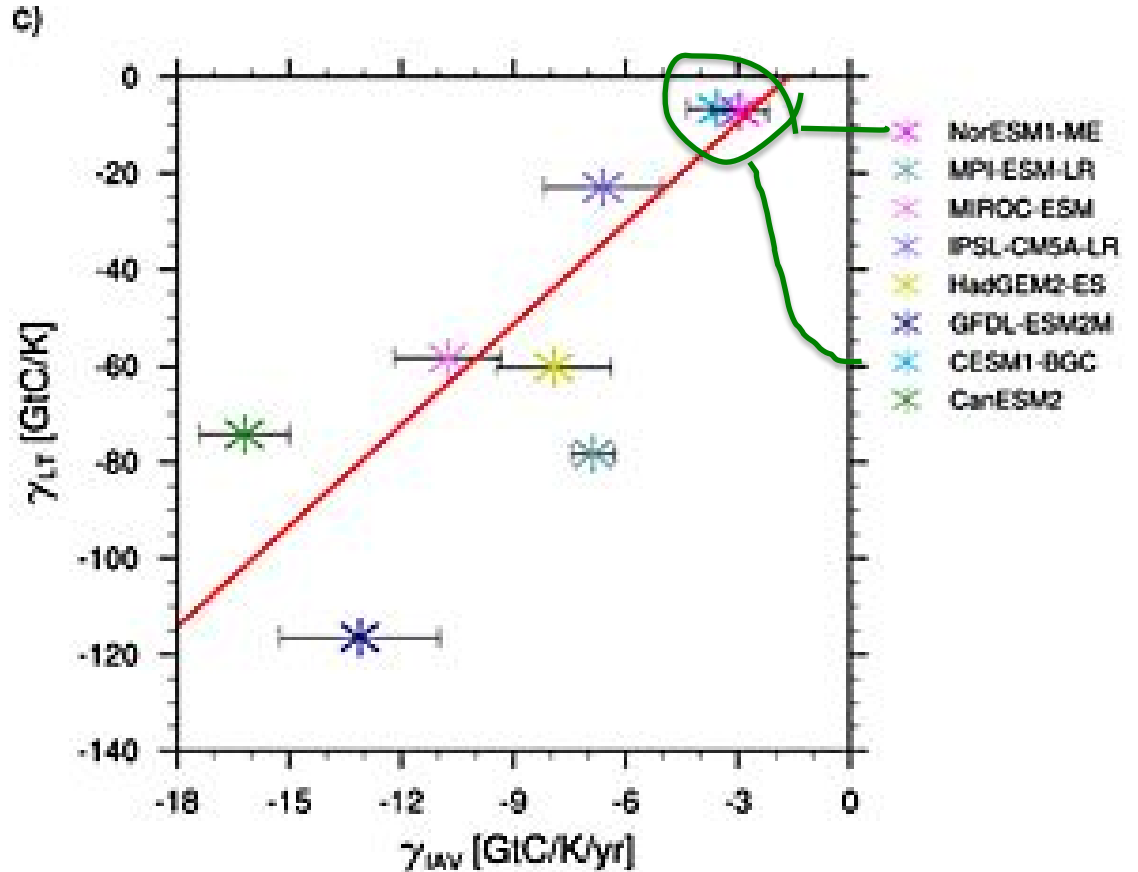


But  
data-mining  
can produce  
spurious  
constraints in  
a small  
sample



Caldwell *et al* (2014)

... and constraints can be artificially enhanced due to replication



## Assumptions

# Bayesian Worldview

IPCC AR5  
Tebaldi et al (2005,2009)

- 1) More **independent** models in agreement implies more confidence in **mean** projection (re-inflation and method to assess intermodel correlation needed)
- 2) Each model is an equally plausible representation of the true system (not generally true, tuning overstates agreement, poor models would overinflate uncertainty)
- 3) Present-day performance can be informative about future behavior (not generally true, general skill metrics are inconsistent, possible use of process-based constraints?)

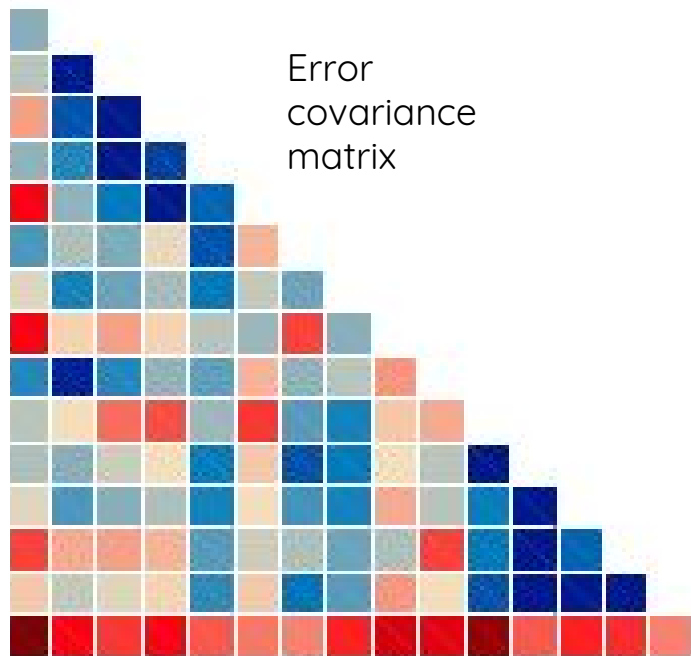
# Worldviews

## Replicate Earth

The ensemble as a whole is a biased representation of reality, which can be transformed to better represent the set of possible states of the true climate system.

Bishop & Abramowitz  
(2013)

A



Error  
covariance  
matrix

$$\mathbf{W} = \frac{\mathbf{A}^{-1}\mathbf{1}}{\mathbf{1}^T \mathbf{A}^{-1} \mathbf{1}}$$

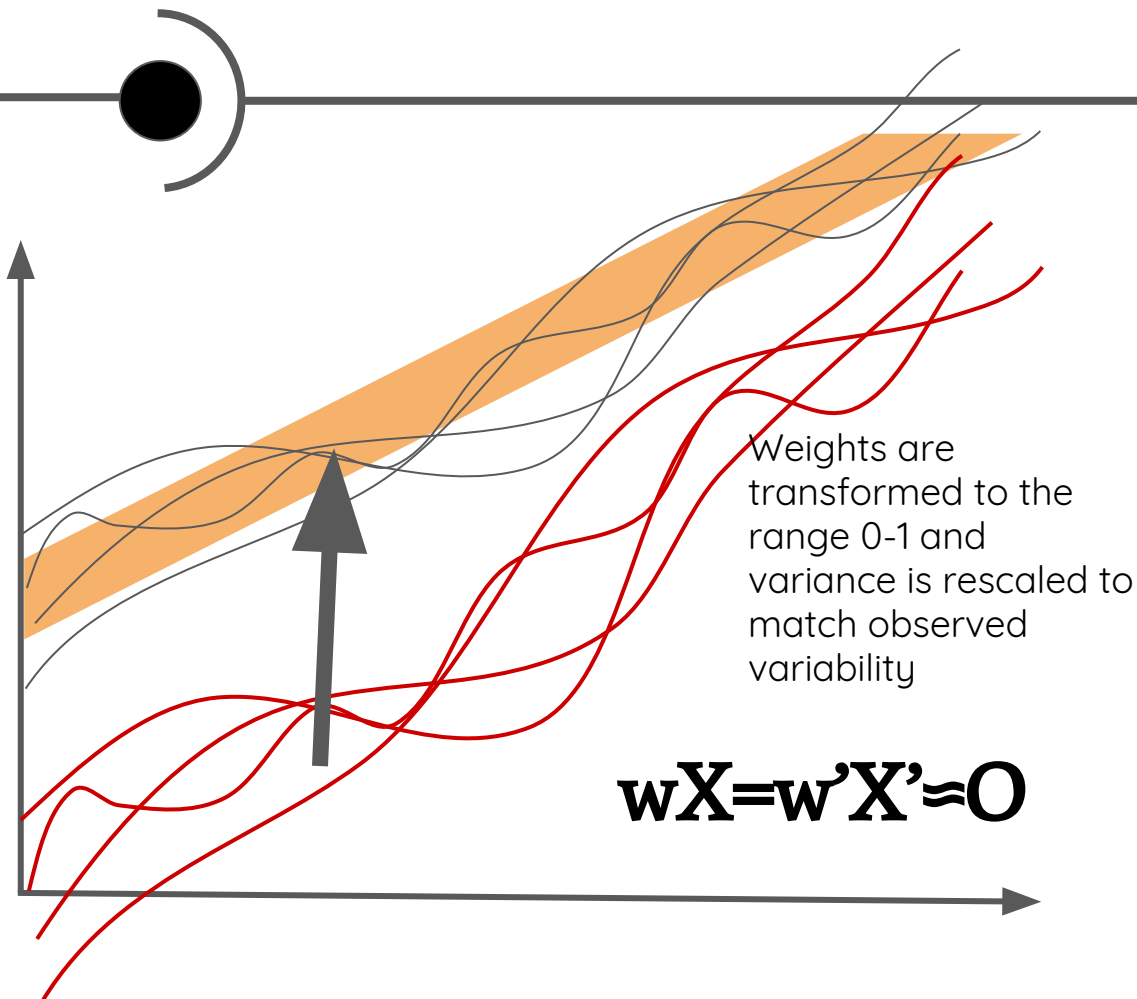
Linear estimator for  
optimal combination  
of models to fit  
observed trajectory  
(automatically  
accounts for  
interdependency)

# Worldviews

## Replicate Earth

The ensemble as a whole is a biased representation of reality, which can be transformed to better represent the set of possible states of the true climate system.

Bishop & Abramowitz  
(2013)





## Assumptions

# Replicate Earth Worldview

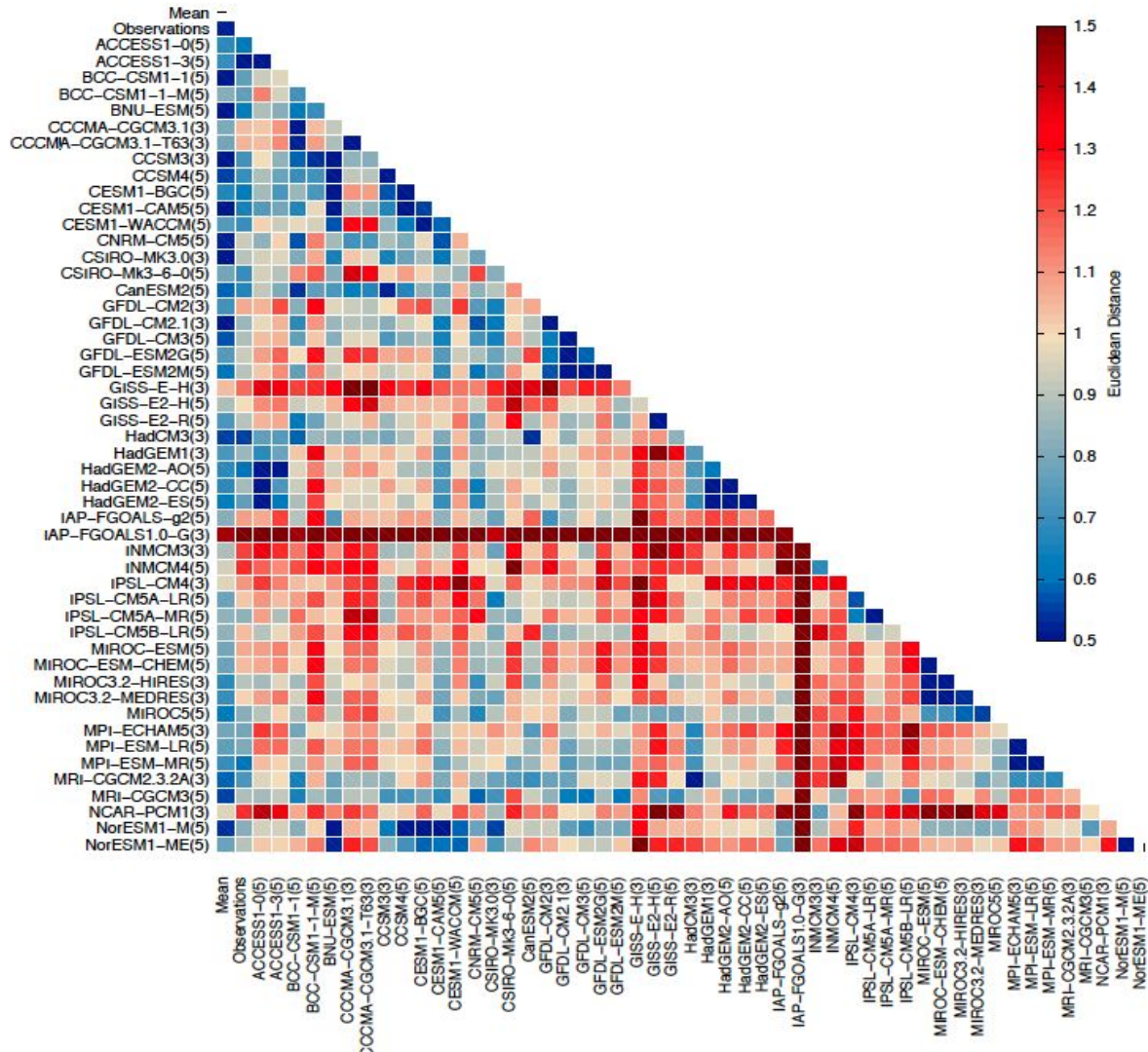
Bishop & Abramowitz  
(2013)

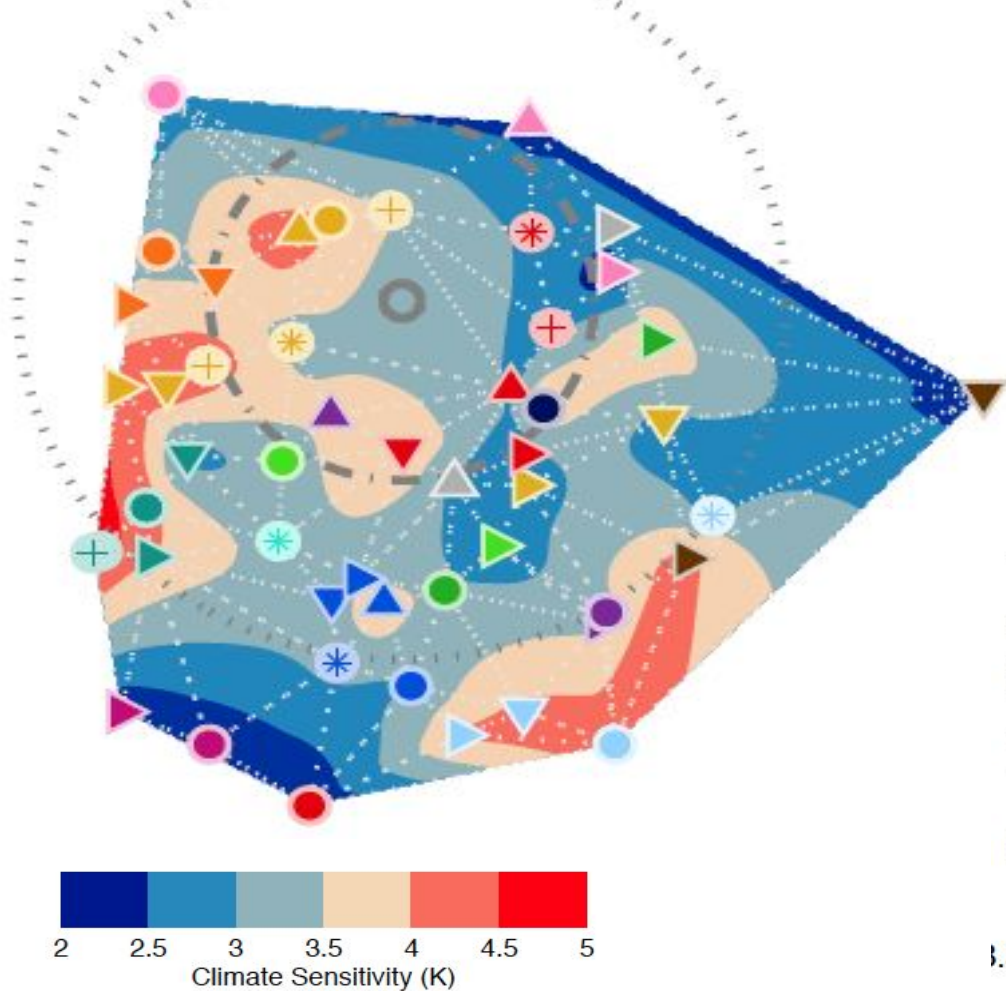
- 1) Models can be linearly combined without constraint to produce an optimal estimate of the true system
- 2) Systematic differences in simulated climate can be rescaled to represent real-world internal variability
- 3) Model interdependency can be accounted for through error correlation.

## Geometric

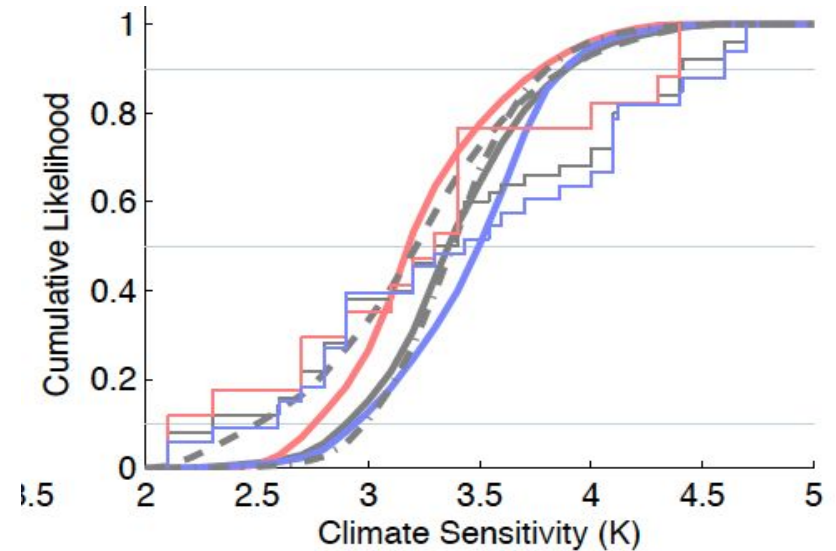
The ensemble is a partially replicated subset of a infinite set of models of varying quality, members of which can be geometrically represented, weighted and interpolated to approximate a distribution of plausible, independent models

Sanderson (2015a,b, 2017)  
Knutti (2017)

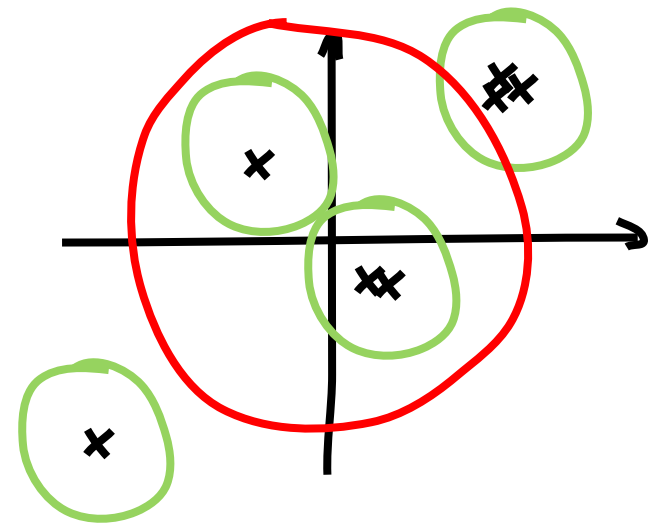
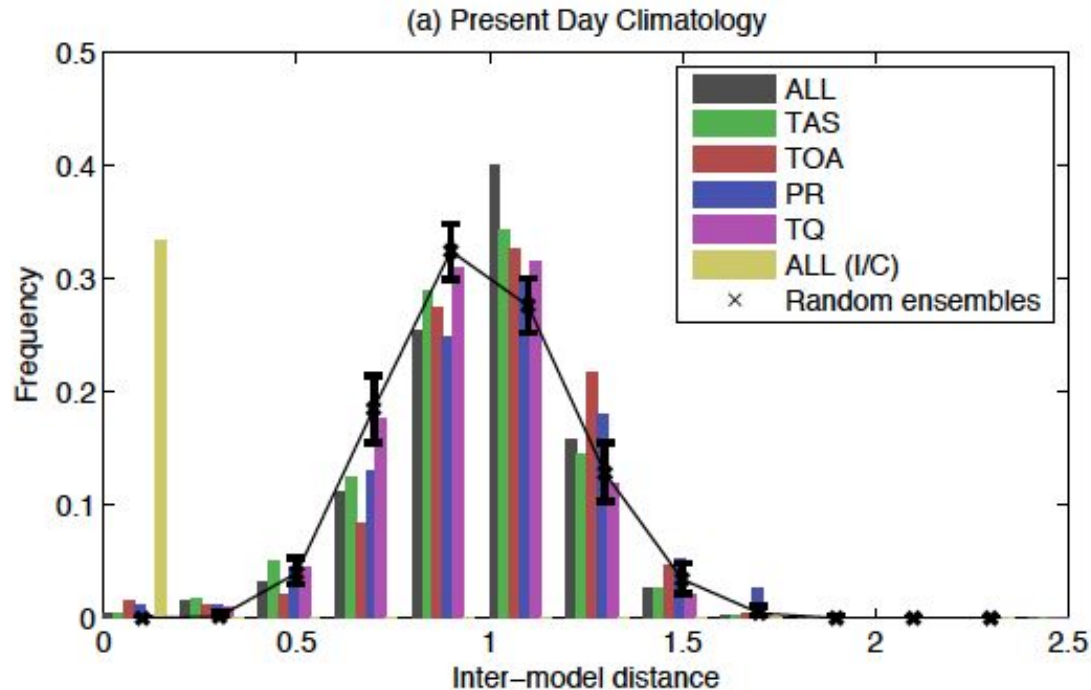




Models are represented in a similarity space, which can be resampled to produce distributions for model properties



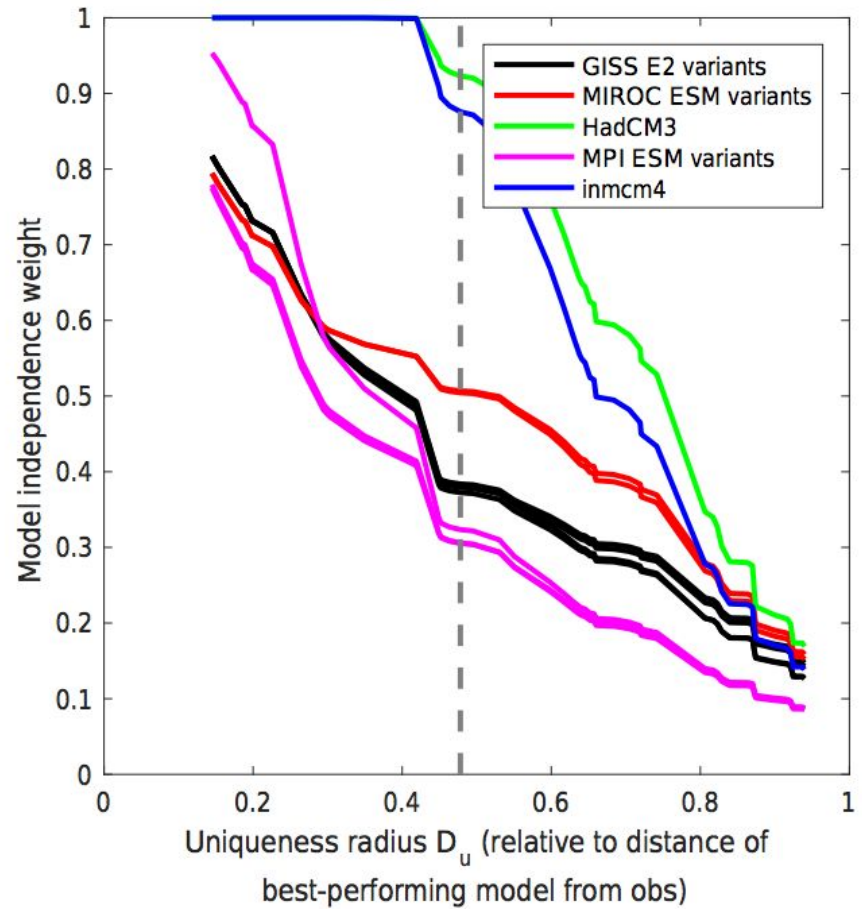
Inter-model: Distances between CMIP mean states are **much** greater than those from initial conditions



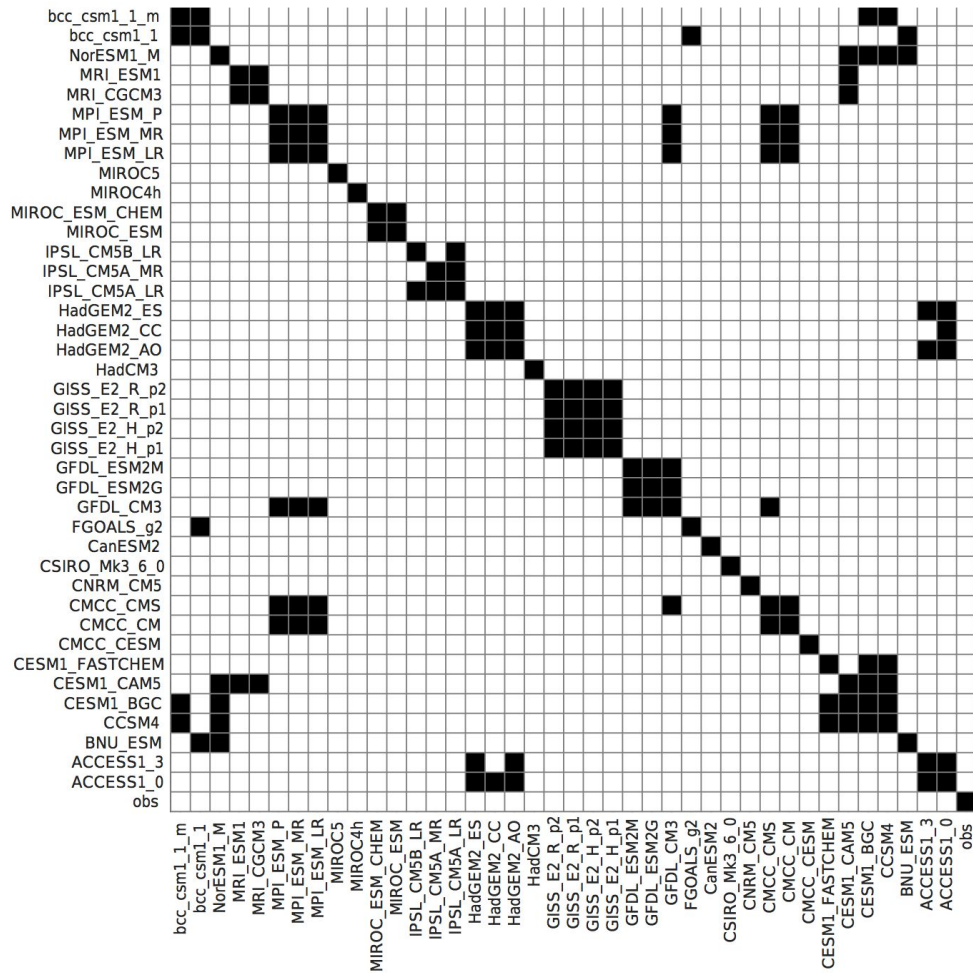
Models in immediate vicinity of other models can be downweighted. Skill is defined by RMSE.

Uniqueness  
weighting  
coefficients make  
intuitive sense

$$w(i) = \frac{e^{-\left(\frac{\delta_{i(obs)}^{20c}}{D_q}\right)^2}}{1 + \sum_{j \neq i}^m e^{-\left(\frac{\delta_{ij}^{20c}}{D_u}\right)^2}}$$

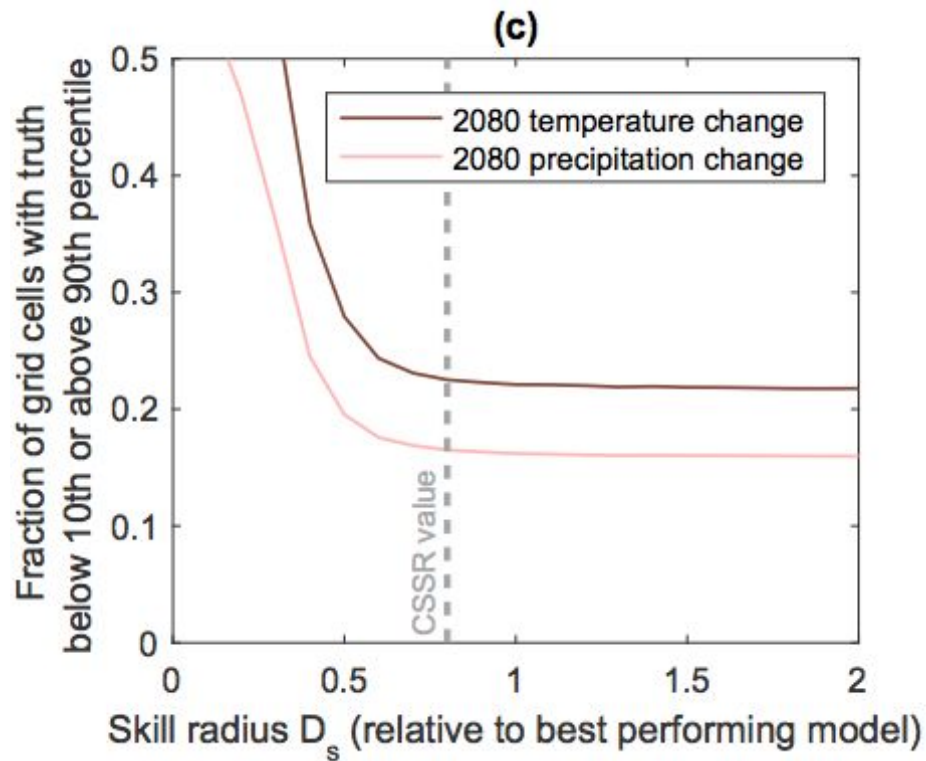
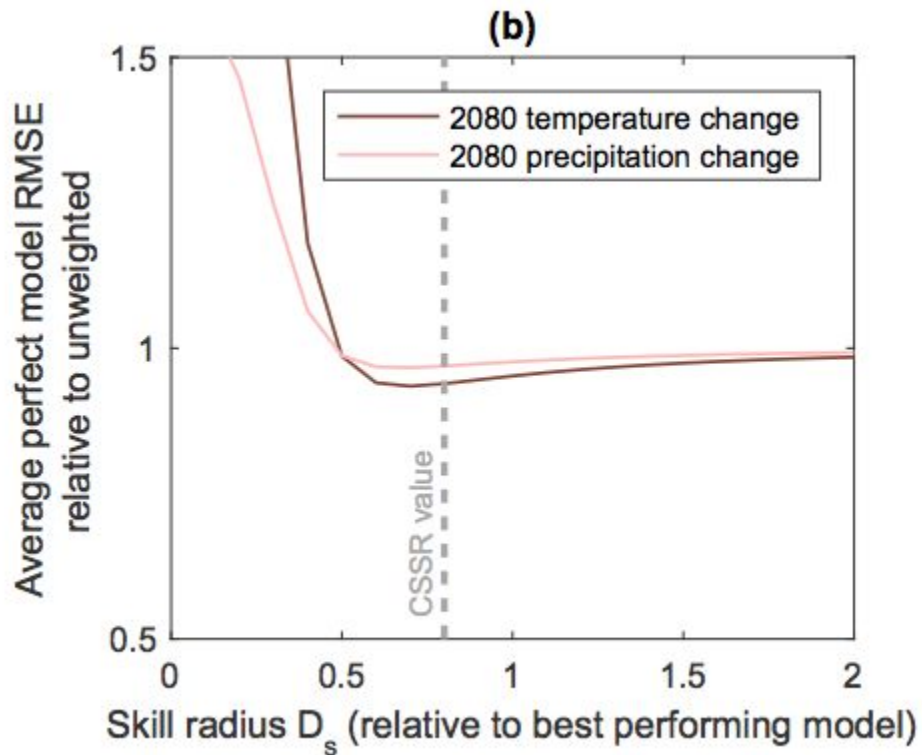




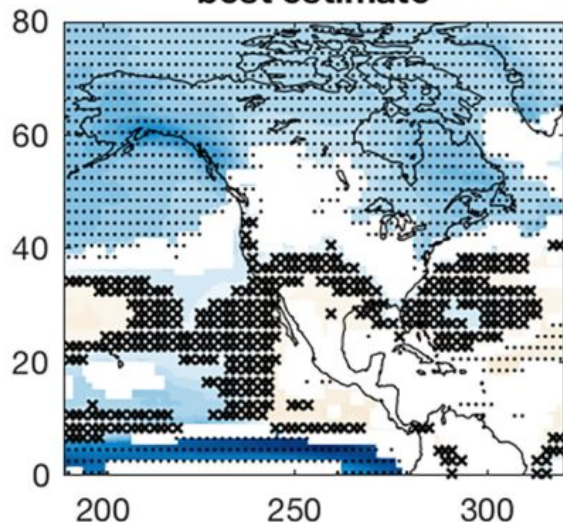


Which provides guidance for identifying strongly interdependent models which should be excluded from out of sample tests.

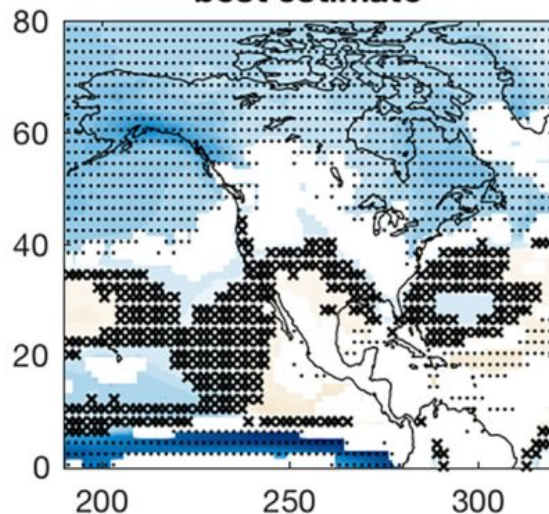
Skill weighting has the potential to improve out-of-sample performance, with risks...



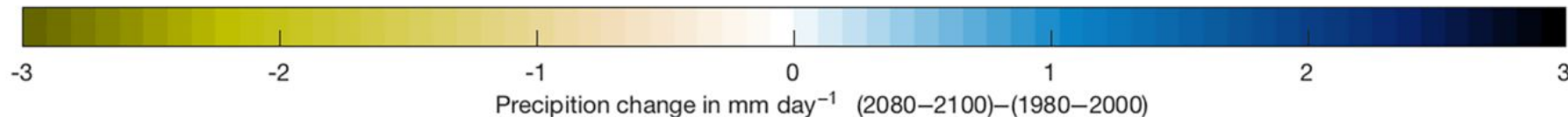
**(a) Unweighted  
best estimate**



**(g) Skill+Independence-weighted  
best estimate**

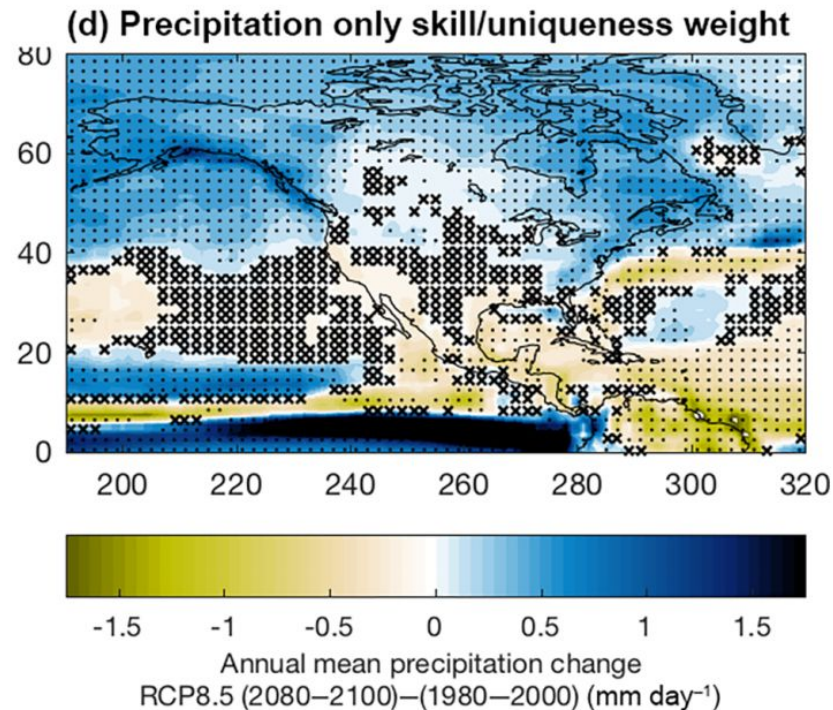
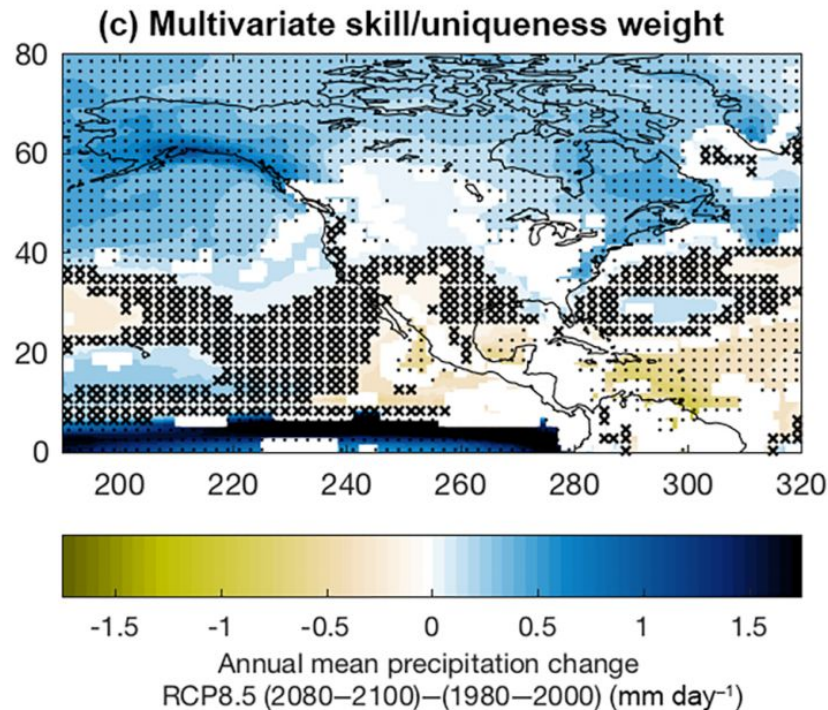


Conservative  
weighting with  
multi-variate  
metrics has little  
effect on  
projections



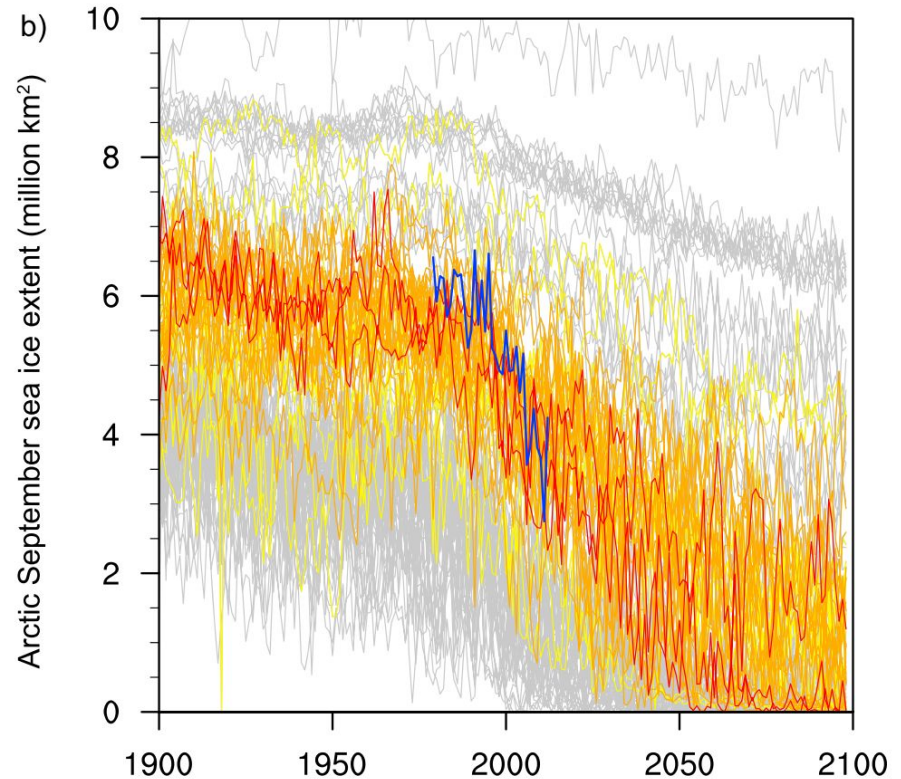


But univariate metrics have a more noticeable effect



Low dimensional  
metric spaces  
provide powerful  
constraints, but lose  
the ability to identify  
interdependency  
through error  
correlation

**Knutti et al (2017)**



## Assumptions

# Geometric Worldview

Sanderson (2015a,b, 2017)  
Knutti (2017)

- 1) CMIP is a subset of possible models of the Earth system. True uncertainty would only be represented by the parent distribution.
- 2) The distribution of inter-model and model-obs distances can provide meaningful weighting information on model interdependency and skill
- 3) Models and observations can be represented in a low dimensional space constructed from diagnostic output and projections can be interpolated to approximate parent distribution

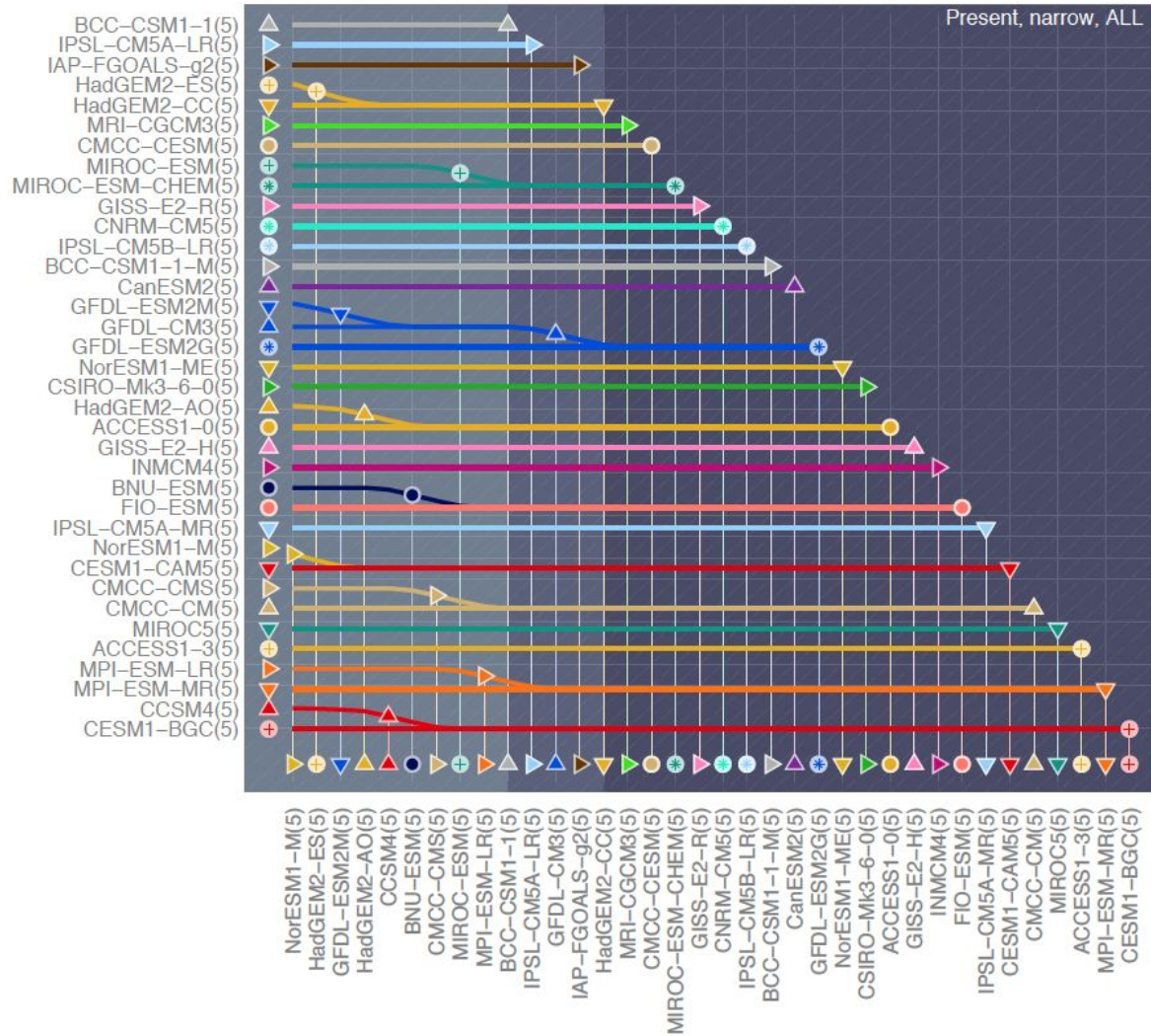
	Bayesian Worldview	Replicate Earth Paradigm	Geometric Worldview
Key strength	Established statistical framework	Remap to earth-like mean and variance	Prediction of unbiased ensemble
Addresses Interdependency?	With modification / error covariance info	Native	Native
Behavior as $N_{\text{models}} \rightarrow \infty$	Posterior converges	Underconstrained regression	Stable
Ad-hoc assumptions	Prior, precision distribution, metrics	Training period, metrics	Metrics, truncation, MDS, sampling prior
Projection within original model range	Yes (for mean)	Not necessarily	Yes
Limit of interpretations	Constraint relevance, over-confidence with common bias	variability/structure, unphysical metamodel, overconfidence	Constraint relevance, scaling/interpolation assumptions
Constraints	Anything	Same as projection	Anything

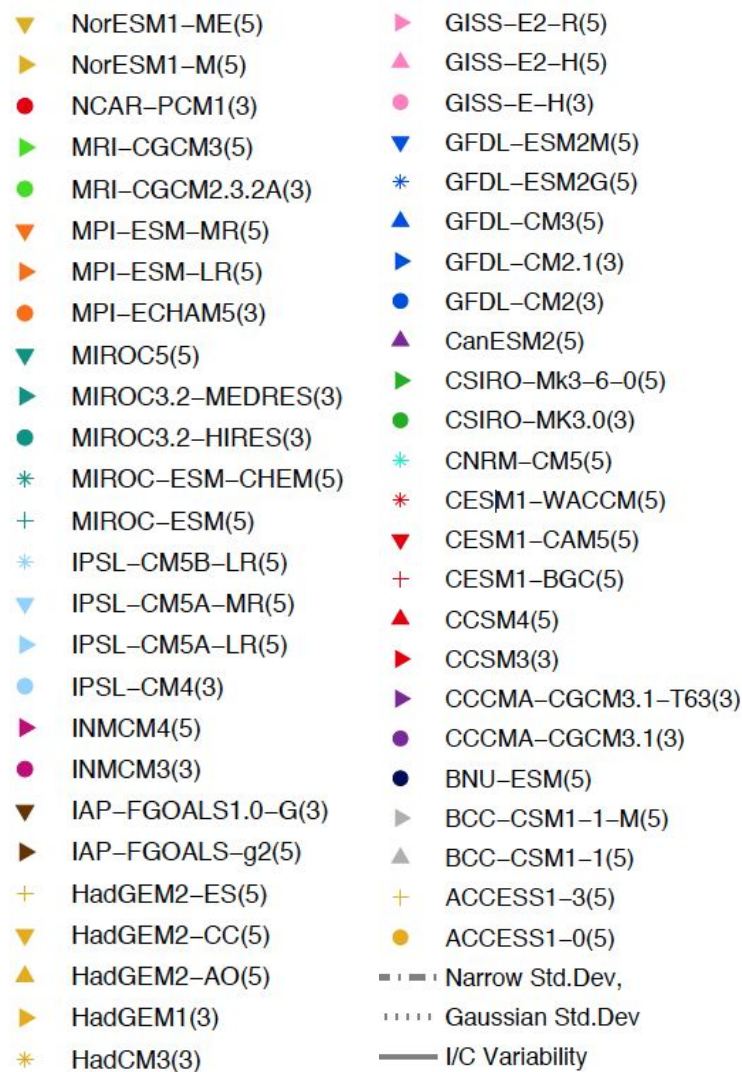
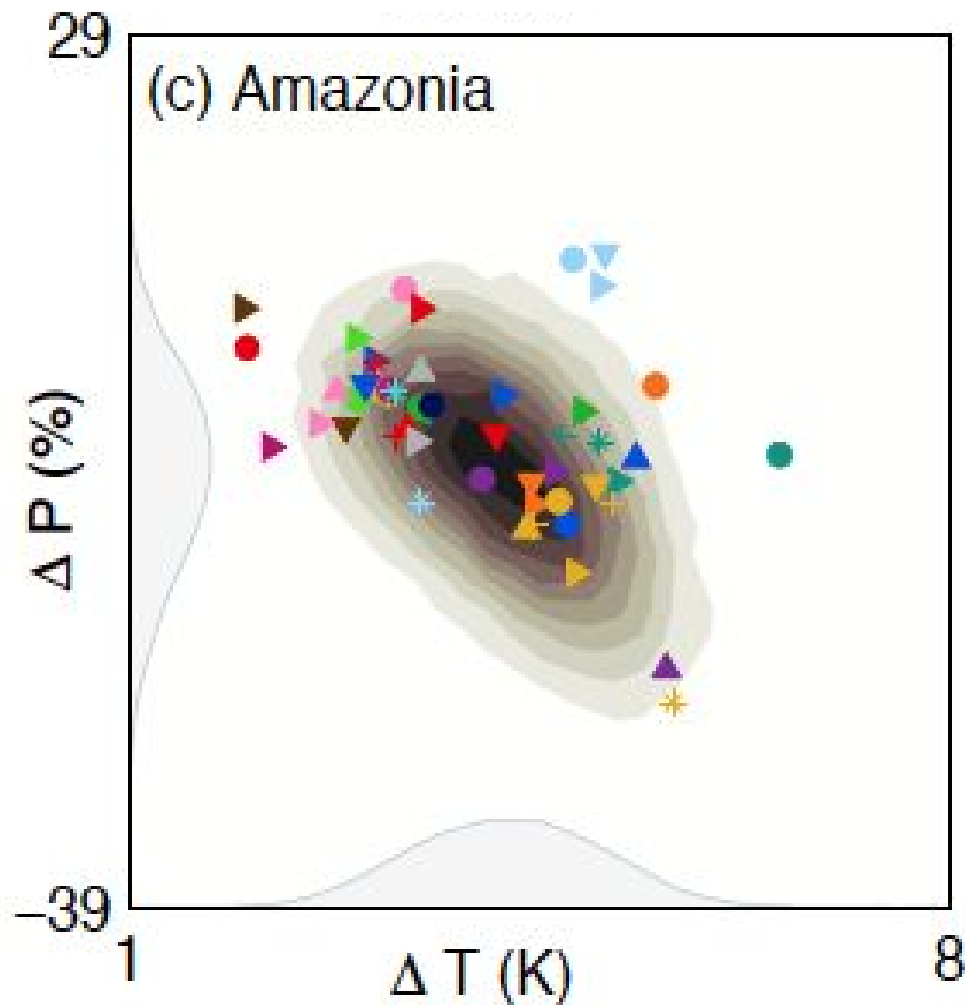
## Next Steps

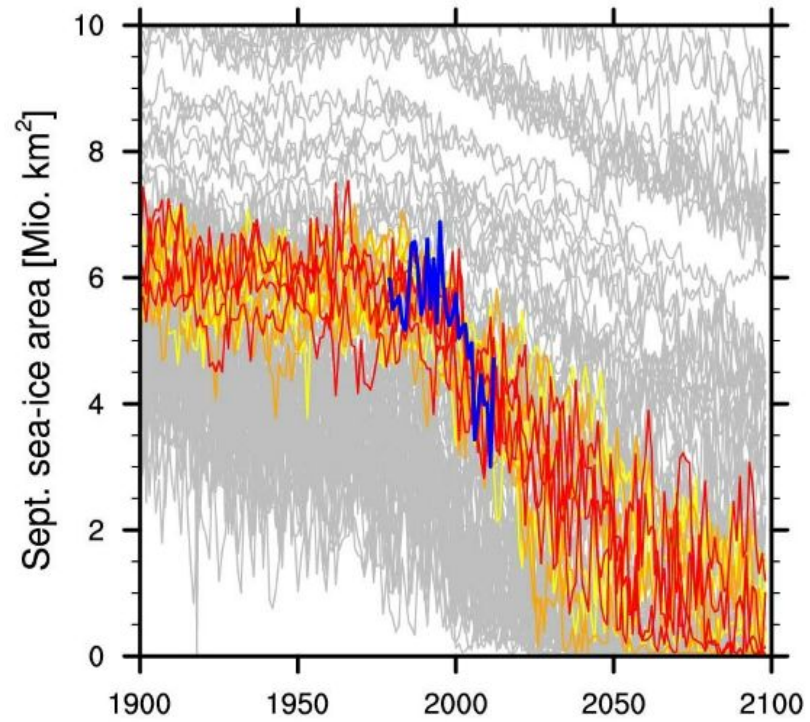
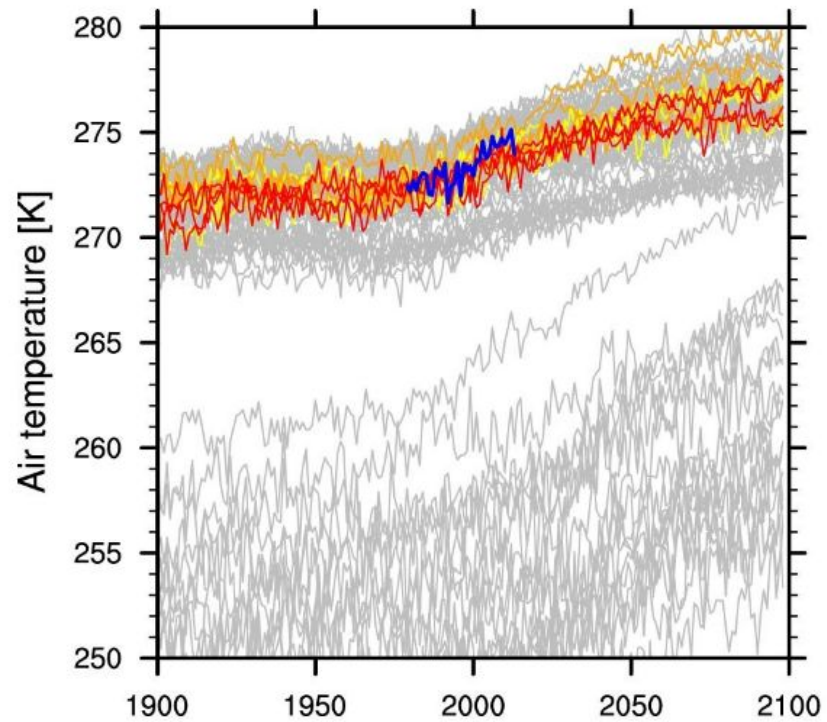
- Greater connection between the emergent constraint / process-based constraint literature and statistical literature
- Better treatment/consideration of internal variability in statistical approaches
- Out of sample testing / validation
- Assess robustness to poor models



Or subsets can  
be created,  
eliminating  
clear  
duplicates first,  
and keeping  
highly  
performing  
models until  
last

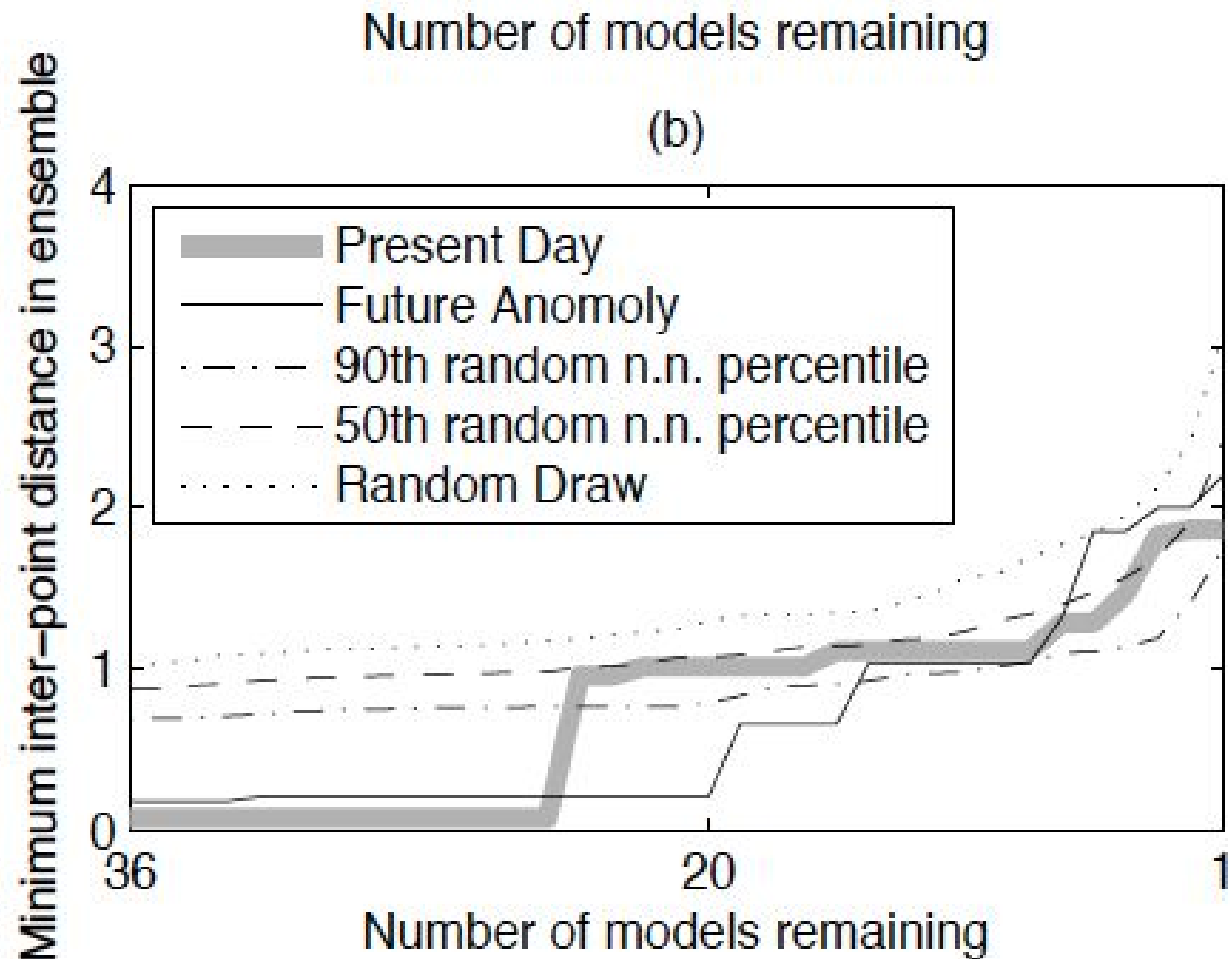




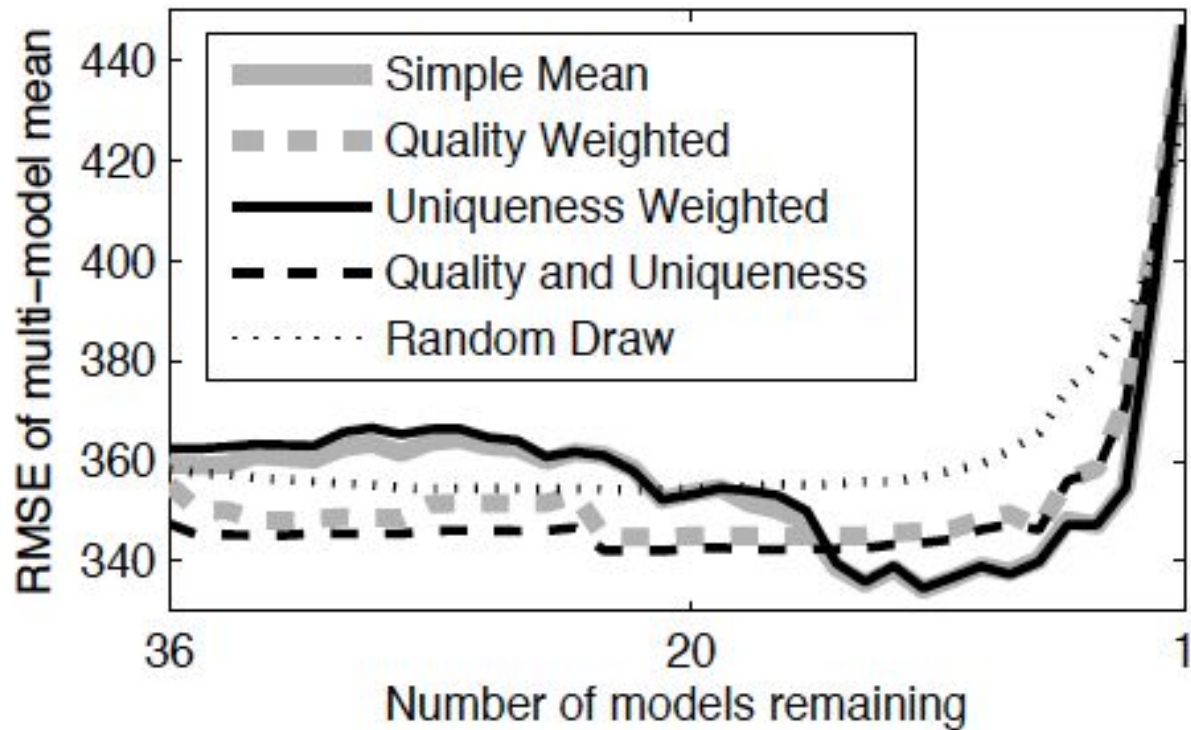




But when to stop?



But when to stop?



Removing replicates

Removing  
poor  
performers

Removing  
better models